

Development of a Polarimetric Radar Forward Operator for the Bayesian Observationally Constrained Statistical-physical Scheme (BOSS)

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Introduction

- We are developing a novel warm-rain microphysics scheme (BOSS, [Poster 119](#)).
- BOSS uses Bayesian inference for robust parameter uncertainty estimation, which facilitates constraint by observations.
- Dual-polarization radar observations will provide a probabilistic constraint on scheme structure and microphysical sensitivities to environmental conditions.
- BOSS can use any combination of prognostic drop size distribution (DSD) moments. Unlike most schemes, however, it does not specify a DSD functional form.
- This necessitates development of a moment-based polarimetric radar forward operator.
- The k^{th} DSD moment (M_k) is

$$M_k \equiv \int_{D_{\min}}^{D_{\max}} N(D) D^k dD$$
 where D_{\min} , D_{\max} : minimum, maximum drop sizes
 $N(D)dD$: number density of drops with diameters D to $D+dD$.
- Choice of prognostic moments will be partly based on the resultant *uncertainty in our forward operator*.
- A given value of M_k can arise from an infinite number of DSDs. Our goal is to assess variability in the *subset of realistic DSDs*.
- Here, we explore analytic DSDs, those produced by a state-of-the-art bin model, and DSDs from ARM disdrometer observations.

Analytic DSDs

- Use the gamma DSD: $N(D) = N_0 D^\mu \exp(-\Lambda D)$
- Compute self-consistent (M_k, M_j) pairs for $k, j=[0, 20]$. From each (M_k, M_j), two DSD parameters (N_0, Λ) are obtained for a wide range of μ similar to what has been observed.
- Compute Z_H, Z_{DR} , and K_{DP} from these DSDs using the T-matrix method ([Fig. 1](#)).

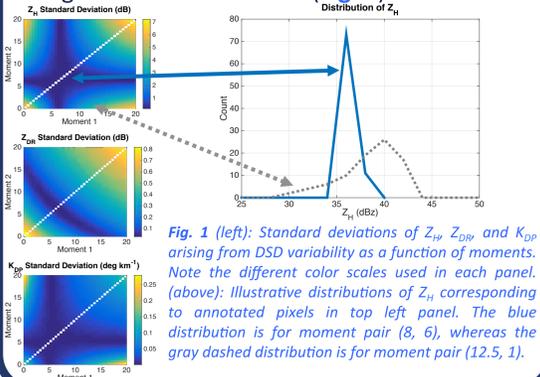


Fig. 1 (left): Standard deviations of Z_H, Z_{DR} , and K_{DP} arising from DSD variability as a function of moments. Note the different color scales used in each panel. (above): Illustrative distributions of Z_H corresponding to annotated pixels in top left panel. The blue distribution is for moment pair (8, 6), whereas the gray dashed distribution is for moment pair (12.5, 1).

- Define a combined variability parameter:

$$\Upsilon \equiv \frac{\sigma_{Z_H}}{\epsilon_{Z_H}} + \frac{\sigma_{Z_{DR}}}{\epsilon_{Z_{DR}}} + \frac{\sigma_{K_{DP}}}{\epsilon_{K_{DP}}}$$

ϵ : expected observational uncertainty
 σ : standard deviation of radar variables for a given set of moments (M_k, M_j) arising from DSD variability

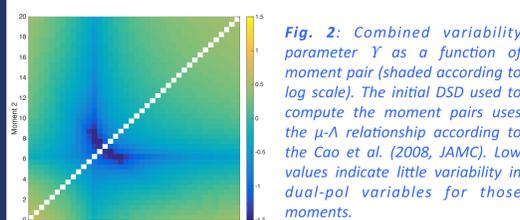


Fig. 2: Combined variability parameter Υ as a function of moment pair (shaded according to log scale). The initial DSD used to compute the moment pairs uses the μ - Λ relationship according to the Cao et al. (2008, JAMC). Low values indicate little variability in dual-pol variables for those moments.

- Fig. 2** suggests prognosing higher moments than traditional schemes in BOSS may improve the utility of polarimetric radar information as a constraint, limiting uncertainty in the forward operator.

Bin Model Simulation Data

- 1D bin microphysical model of Prat and Barros (2007, JAMC) used. Simulations run for 60 minutes (output $\Delta t = 1$ min) in a 3-km-tall domain ($\Delta z = 10$ m). Normalized gamma DSDs initialized at domain top with the following parameter ranges:
 - D_0 : 0.2 mm to 4 mm
 - N_w : 100 to 80000 $\text{mm}^{-1} \text{m}^{-3}$
 - μ : -1 to 10
- Restrict to $0.01 \text{ mm hr}^{-1} < R < 500 \text{ mm hr}^{-1}$, resulting in 10742 simulations.
- DSDs are taken at every output time and height, resulting approximately **199 million DSDs**.

ARM Disdrometer Data

- PARSIVEL-2 and 2D video disdrometer data from ARM sites around the world are used.
 - PARSIVEL-2 (15.5 million DSDs)**
 - SGP (2006-2016)
 - TWP (2006-2015)
 - 2DVD (6.1 million DSDs)**
 - SGP (2011-2016)
 - ENA (2014-2016)
 - TWP (2011-2015)
 - GAN (DYNAMO-AMIE; 10/2011-2/2012)
 - TMP (BAECC; 2/2014-9/2014)

Combined Data: Results

- 220.7 million "realistic" DSDs**; moments and dual-pol variables computed for each ([Fig. 3](#)).

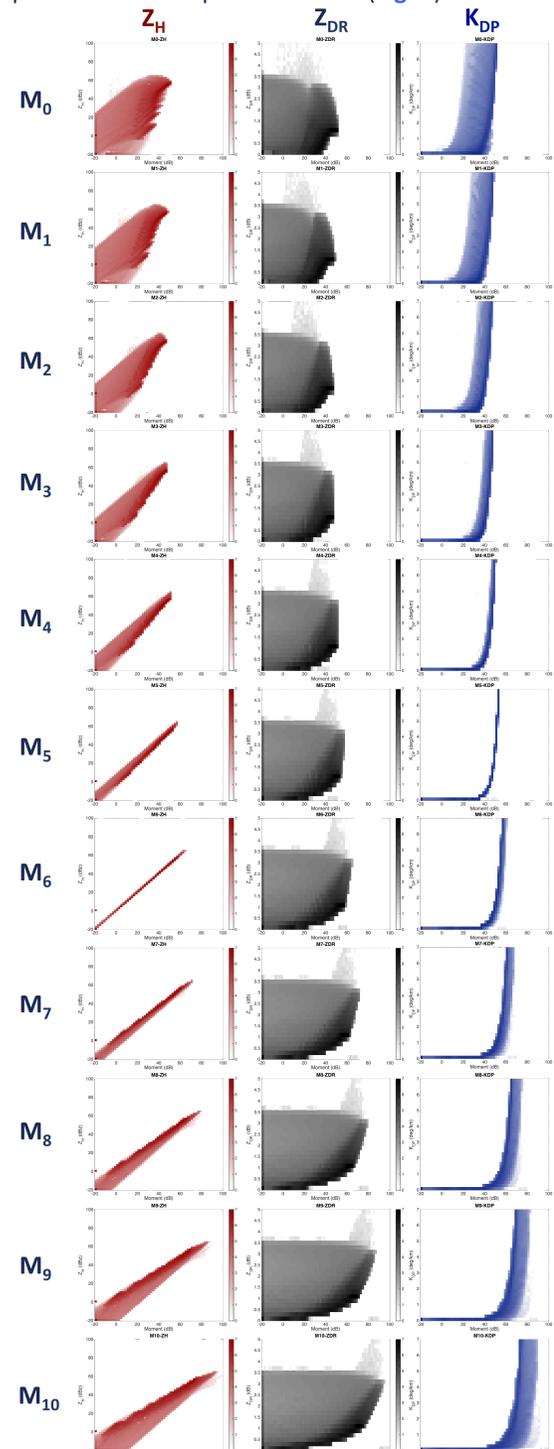


Fig. 3: 2D histograms showing the relationship between moments (rows) and the dual-polarization radar variables Z_H (red, left), Z_{DR} (black, middle), and K_{DP} (blue, right). Occurrence is shaded according to log scale. The combined dataset is used.

- For the 2-moment BOSS, we desire the pair of predicted moments (M_k, M_j) that minimizes uncertainty in the forward operator (i.e., *for which pair of moments do the dual-polarization radar variables provide the most information?*)

- Compute the distribution-weighted standard deviation for each radar variable X :

$$\xi \equiv \sum_m^M \sum_n^N \sigma_X [M_k^{(m)}, M_j^{(n)}] \times P [M_k^{(m)}, M_j^{(n)}]$$

where P is the joint pdf of M_k and M_j , which are discretized into M and N bins, respectively. Results for all (k, j) pairs considered are shown in [Fig. 4](#).

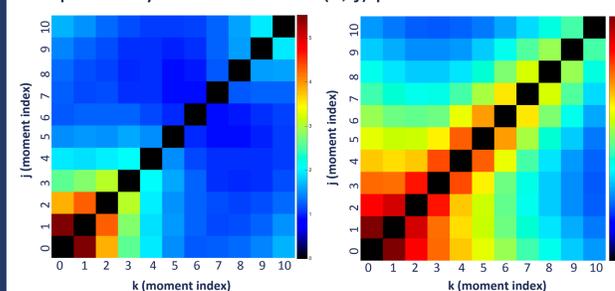


Fig. 4: ξ for (left) Z_H , and (right) Z_{DR} as a function of moment indices k and j , shaded according to scale in dB. Combinations of moments (k, j) that have the least uncertainty in a given radar variable have lower values of bivariate ξ .

- Formulate the forward operator for a number of different moment pairs (for 2-moment BOSS) or triads (for 3-moment BOSS). This will be in the form of a look-up table. [Fig. 5](#) shows an example of what this looks like for (M_6, M_8).

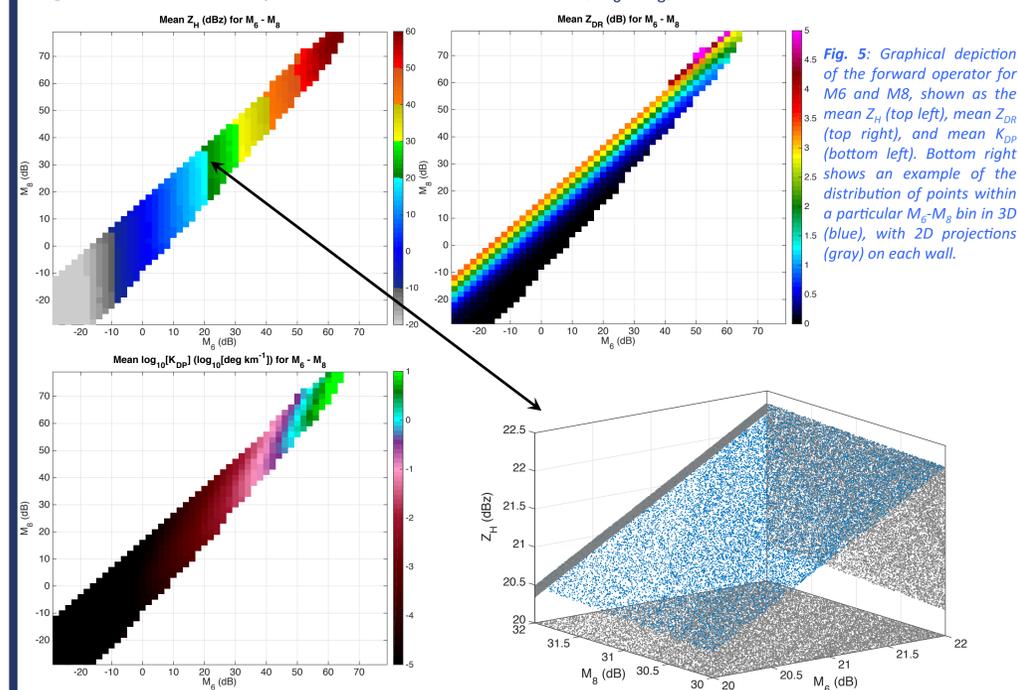


Fig. 5: Graphical depiction of the forward operator for M_6 and M_8 , shown as the mean Z_H (top left), mean Z_{DR} (top right), and mean K_{DP} (bottom left). Bottom right shows an example of the distribution of points within a particular M_6 - M_8 bin in 3D (blue), with 2D projections (gray) on each wall.

- The forward operator must also account for the uncertainty within a given M_k - M_j bin. Thus, the look-up table will include not only the mean values of Z_H, Z_{DR} , and K_{DP} in each bin, but also the de-trended standard deviation of Z_H, Z_{DR} , and K_{DP} within a bin, as well as the distribution skewness, and covariances between the polarimetric radar variables.



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